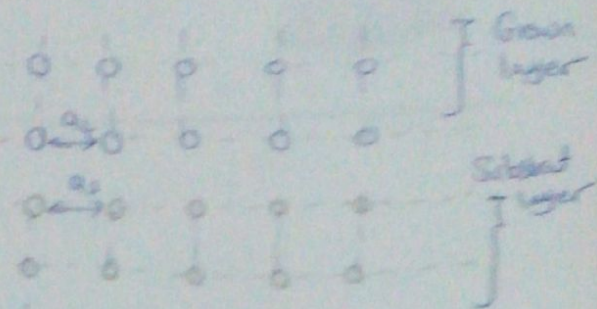


## Sec (7)

Remember: Lattice matched Hetero structure  
Used For Radiative transitions

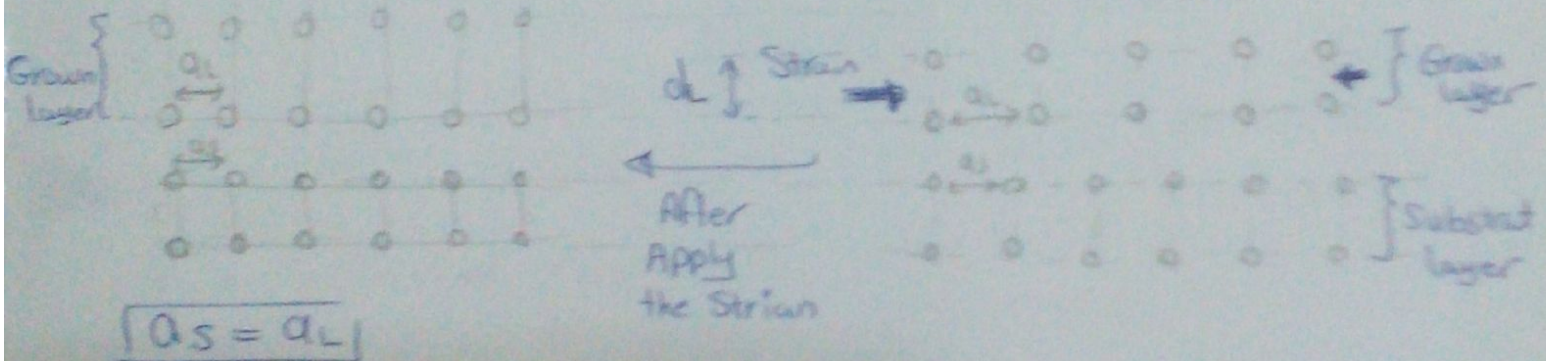
Lattice Matched  
Hetero structure  
[Because  $a_s = a_L$ ]



## 2] Strained layer epitaxy

if  $a_s \neq a_L \rightarrow$  [lattice mismatch] ~~not~~

To fix this problem  
+ Apply strain to the Grown layer  
from sides



لا حظ ان طول ال Grown layer

كانت اما ضغط حرد زاد من الجهد

الكار = بى الصلا

ما هو القدر الواجب توازنه حتى يمكن استمرار نمو الطبقة المتناغمة

Condition to use strained layers

$$d_L < d_{critical}$$

where:  $d_c = \frac{a_s}{2|\epsilon|}$

&  $\epsilon = \frac{a_L - a_s}{a_L}$



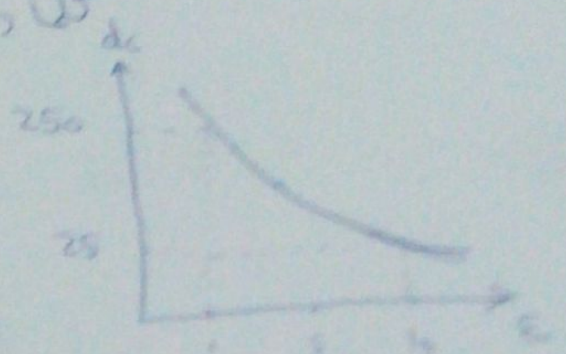
$\epsilon \rightarrow$  mismatch parameter  $\rightarrow$  if  $\epsilon = 0 \Rightarrow a_s = a_L$  Matched  
 $\epsilon \neq 0 \rightarrow a_s \neq a_L \rightarrow$  Mismatched

Ex: For Semiconductor  $a_s = 5 \text{ \AA}$  if  $\epsilon = 1\% \rightarrow 10\%$   
 $\downarrow \quad \downarrow$   
 $0.01 \quad 0.1$

$$\text{at } \epsilon = 0.01 \rightarrow d_c = \frac{5 \text{ \AA}}{2 \times 0.01} = 250 \text{ \AA}$$

$$\epsilon = 0.1 \rightarrow d_c = \frac{5}{2 \times 0.1} = 25 \text{ \AA}$$

$d_c$  ← "  $\epsilon$  " Mismatch at,  $d_c$



Ex: To build optical Source from  $\text{In}_x\text{Ga}_{1-x}\text{As} / \text{GaAs}$

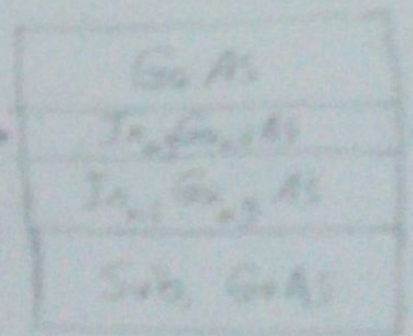
at  $x=0 \rightarrow \text{GaAs} \rightarrow a = 5.65 \text{ \AA}$

$x=1 \rightarrow \text{InAs} \rightarrow a = 5.87 \text{ \AA}$

$\hookrightarrow$  mismatch lattice mismatch can be modified by compressive strain only when

$$d_L < d_c$$

Compressive strain



Optical source

في مكثف (5) ارمال - اقترح تصميم

معك تصميم الدرع الى يمين و يكتب الشرط



# 1. Interaction of light with matter

→ What is de Broglie wavelength?

$$\lambda = \frac{2\pi}{k} = \frac{2\pi\hbar}{p} = \frac{h}{\sqrt{2m^*E}}$$

Ex: Compute  $\lambda$  de Broglie wavelength at  $T = 300^\circ K$  &  $m_c^* = 0.067m_0$

$$\lambda = \frac{h}{\sqrt{2m_c^*E_{KE}}}$$

$$E_{KE} = \frac{1}{2}m^*v^2$$

$$= \frac{p^2}{2m^*}$$

$$\therefore p = \sqrt{2m^*E}$$

effective mass

$$E_{KE} = kT = 0.025 \text{ eV}$$

$$\lambda = \frac{h}{\sqrt{2 \times 0.067 \times m_0 \times 0.025 \text{ eV}}} = 300 \text{ \AA}$$

↑  
Calculator

So if we use  $d_L$  (in Double Heterostructure)  $= 100 \text{ \AA}$   
 → This structure will be Quantum well structure.

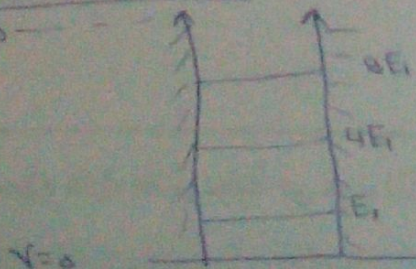
→ What will happen to Allowed States in Active layer if its thickness decrease?

Remember Particle in the Box

$$E = \frac{\hbar^2}{2m} \left( \frac{n\pi}{L} \right)^2$$

$$E_1 = \frac{\hbar^2}{2m} \left( \frac{\pi}{L} \right)^2$$

$$E_2 = 4E_1$$



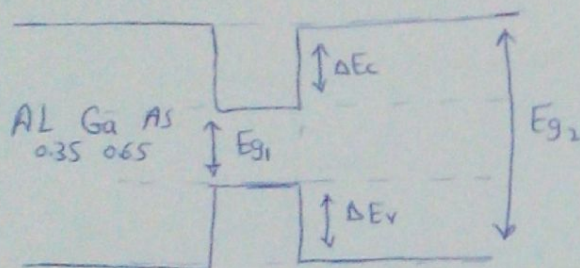


## Interaction of Light with matter:

Ex: Find Emission wavelength Can be controlled by change the thickness of the, layer?

For  $Al_{0.35}Ga_{0.65}As / GaAs / Al_{0.35}Ga_{0.65}As$

~Sol~



For  $Al_{0.35}Ga_{0.65}As$

$$E_{g2} = 1.424 + 1.242 \times$$

$$E_{g2} = 1.86 \text{ eV}$$

For  $GaAs$

$$E_{g1} = 1.42 \text{ eV}$$

Note For most optoelectronic material

$$\Delta E_c = 0.65 \Delta E_g$$

$$\Delta E_v = 0.35 \Delta E_g$$

$$\Delta E_g = 1.86 - 1.42 = 0.44 \text{ eV}$$

$$\therefore \Delta E_c = 0.29 \text{ eV}$$

$$\Delta E_v = 0.15 \text{ eV}$$

Range For emission wavelength:

$$\text{From } E_{g2} = 1.86 \text{ eV} \rightarrow \lambda_2 = 0.67 \mu\text{m}$$

$$E_{g1} = 1.42 \text{ eV} \rightarrow \lambda_1 = 0.87 \mu\text{m}$$

$$\lambda \rightarrow 0.67 \mu\text{m} \rightarrow 0.87 \mu\text{m}$$



Q (4)

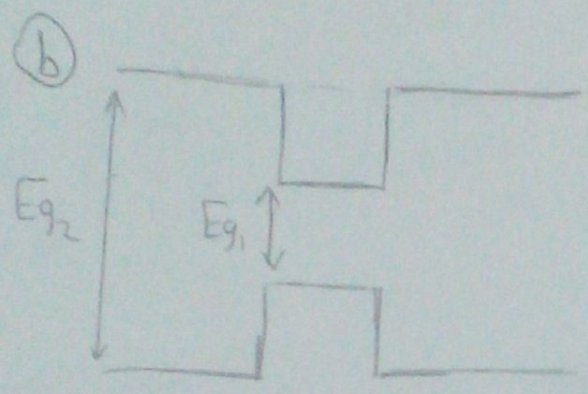
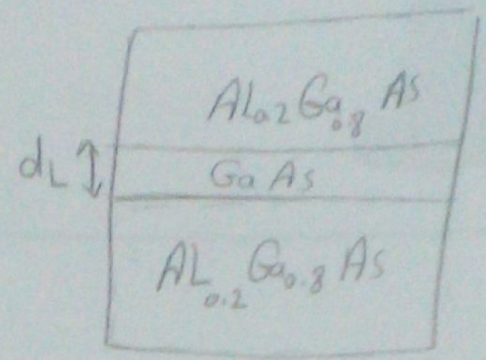
Similar Example  
in page 6

a) Quantum Well structure

$$d_L < \lambda_e$$

$$\lambda_e = 300 \text{ \AA}$$

de Broglie wavelength



$$E_{g1} |_{\text{GaAs}} = 1.42$$

$$E_{g2} |_{\text{Al}_{0.2}\text{Ga}_{0.8}\text{As}} = 1.424 + 1.2(0.2)$$

$$E_{g2} = 1.67$$

(c)

Application

→ Laser Source (To explain the operation)  
see page 5

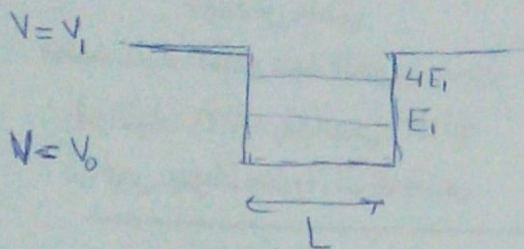
d) Max. and Min. wavelength =

$$E_{g2} = 1.67 \text{ eV} \rightarrow \lambda_2 = \frac{1.24}{1.67} = 0.74 \mu\text{m}$$

$$E_{g1} = 1.42 \text{ eV} \rightarrow \lambda_1 = \frac{1.24}{1.42} = 0.87 \mu\text{m}$$



But in Finite Quantum well

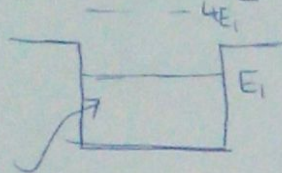


if  $L \rightarrow$  decrease

$$E_1 \uparrow = \frac{\hbar^2}{2m} \left( \frac{\pi}{L} \right)^2$$

↑  $E_1$  قىممى كىچىك

← يىقىنلاشقانلىقى  
shift  
دېگەنلىك



يىقىنلاشقانلىقى

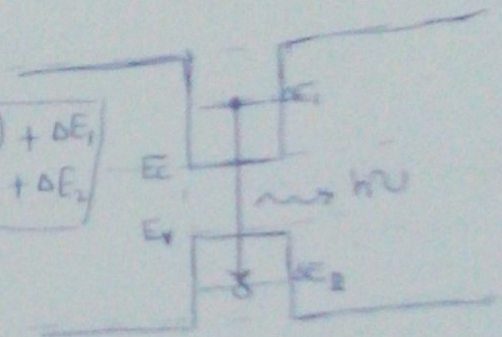
التماسىنىڭ

thickness

$\lambda$  بىر تەرەپتىن

de one allowed state

$$E_{g \text{ effective}} = (E_c - E_v) + \Delta E_1 + \Delta E_2$$



laser  
Source

← photon  
with single  
freq.

Quantum well structure

# Quantum well structure used in Laser Source

$$E_{g \text{ effective}} = (E_c - E_v) + \Delta E_1 + \Delta E_2$$

→ Band Gap Controlled by Sandwiched layer



# Interaction of light with matters

Absorption

Emission

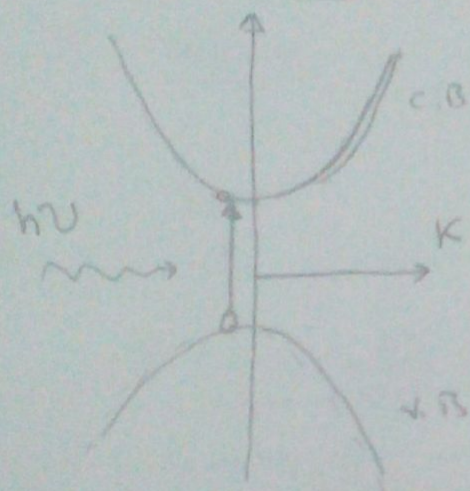
Spontaneous emission

Stimulated emission

## 1] Absorption

## 2] Spontaneous

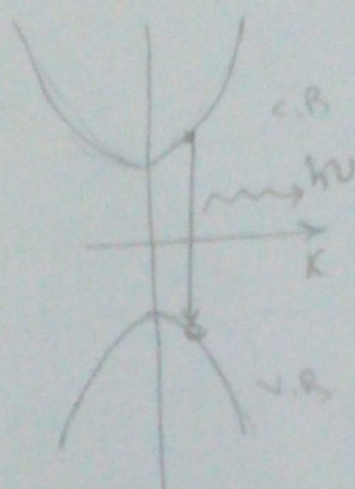
## 3] Stimulated



Input photon create hole-electron pair.

# Application

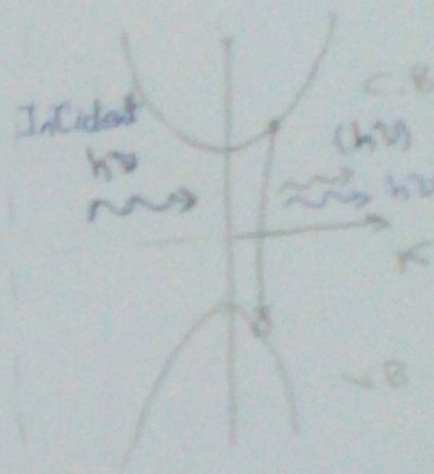
photo detector



Transition of electron from c.B  $\rightarrow$  v.B create photon

# Application

LED



Incident photon (in phase) with the resulted photon [from spontaneous emission]

# Application

Laser



## 1] Conservation of Energy

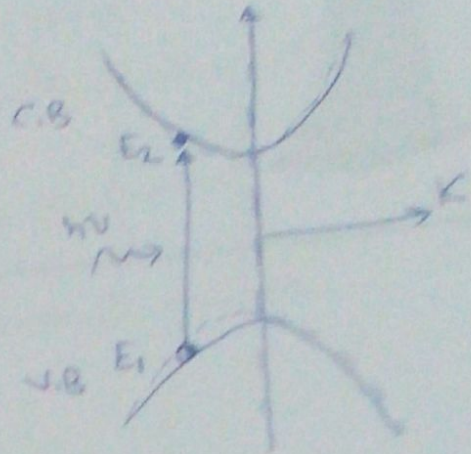
absorber

In Absorption

$$h\nu = E_2 - E_1$$

$$\therefore E_2 = E_1 + h\nu$$

↑ Final Energy     ↑ Initial     ↑ photon



or emission

$$E_2 - E_1 = h\nu \rightarrow \boxed{E_2 = h\nu + E_1}$$

## 2] Conservation of momentum

momentum  $\rightarrow P_{e \text{ initial (1)}} = \hbar k_1$

$$P_{e \text{ final (2)}} = \hbar k_2$$

$$\vec{P}_2 = \vec{P}_1 + \vec{P}_{ph}$$

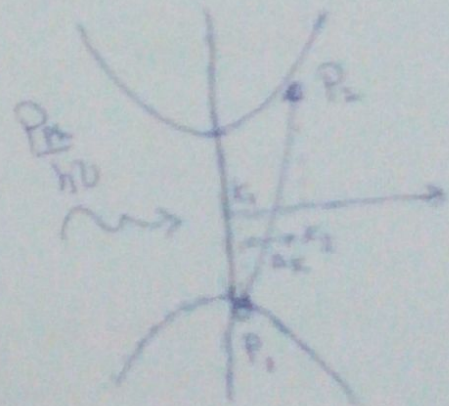
$$\hbar k_2 = \hbar k_1 + \hbar k_{ph}$$

$$k_2 = k_1 + k_{ph}$$

↑  
neglected

$$\therefore \boxed{k_2 = k_1} \rightarrow \Delta k = 0 \rightarrow \text{vertical transition}$$

↑  
Momentum is conserved



For optical Communication

$$\lambda = 0.5 \rightarrow 1.5 \mu\text{m}$$

$$\text{let } \lambda = 1 \mu\text{m} = 10,000 \text{ \AA}$$

$$k_{ph} = \frac{2\pi}{10,000}$$

For electron  $\lambda_e = 10 - 100 \text{ \AA}$

$$k_1, k_2 = \frac{2\pi}{10}$$

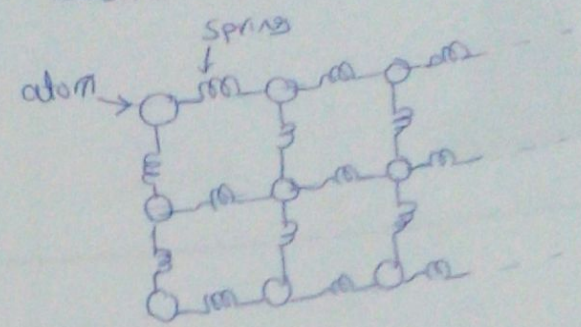
$$k_{ph} \ll k_e$$



Note

↳ Bonds between atom is elastic bonds (not static)

الذرات تتحرك نتيجة اهتزازها

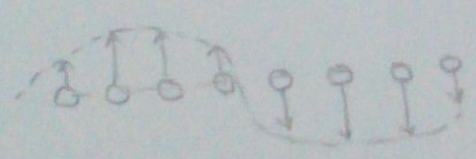


↳ What is Phonon?

↳ ~~Quant~~ Quanta of lattice vibrations

↳ Types of Phonon?

Acoustic phonon

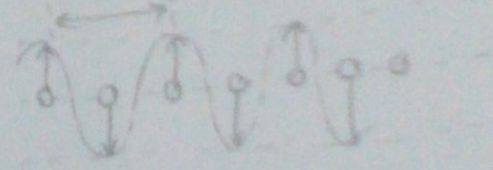


↳ Group of atoms displaced in same direction

↳  $\lambda \gg a \rightarrow f \downarrow \downarrow$

Optical phonon

$\lambda = 2a \rightarrow \text{very small}$



الذرات يهتز في اتجاهات متعاكسة

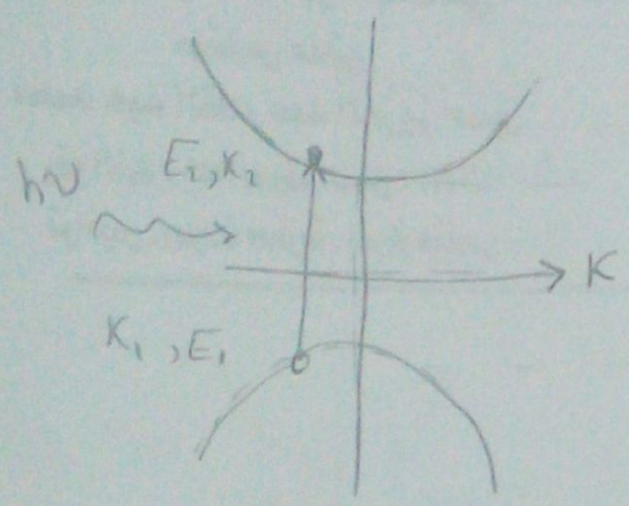
↳ Atoms displaced in opposite direction

↳  $\lambda = 2a \rightarrow \text{very small}$

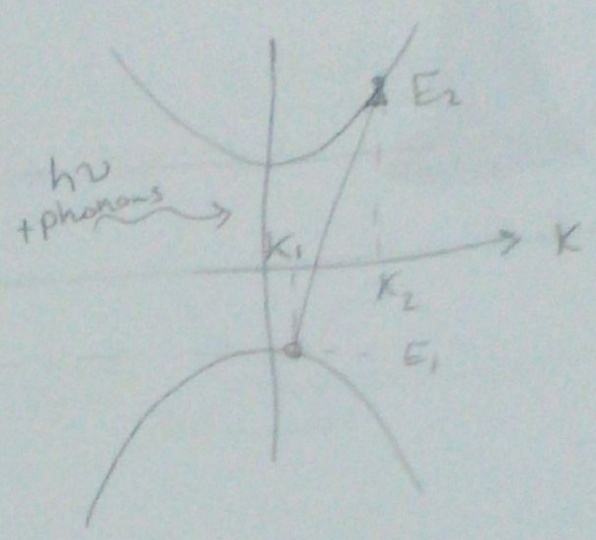
↳  $f_{\text{optical}} \gg f_{\text{acoustic}}$



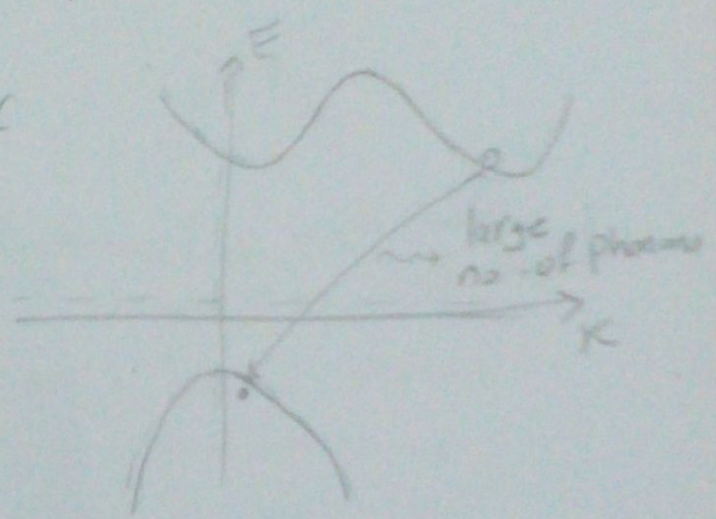
Photon Assisted transition	Phonon Assisted transition
----------------------------	----------------------------



↪ Vertical transition  
(No change in momentum)



OR



↪ Initial state and Final state has different K

Photon	Phonon
--------	--------

Define : Quanta of light

↪ Quanta of vibrations

Energy      1 eV → 3 eV

↪ 10 meV → 70 meV

Wavelength       $\lambda = 0.5 \mu m \rightarrow 1.5 \mu m$

↪  $\lambda = 10 \text{ \AA} \rightarrow 100 \text{ \AA}$

↪ Probability of radiation photons is large in direct Semiconductor

↪ probability of radiation phonons is large in Indirect Semiconductor

↪ نفس الرسومات التي في صفحة 11

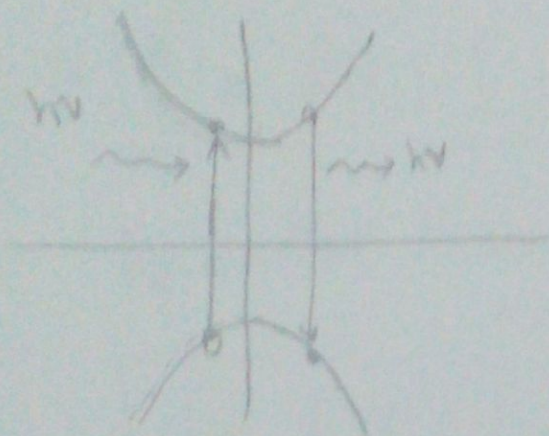
↪ نفس الرسومات التي في صفحة 11



## C] Radiative & Non-radiative :

### Radiative

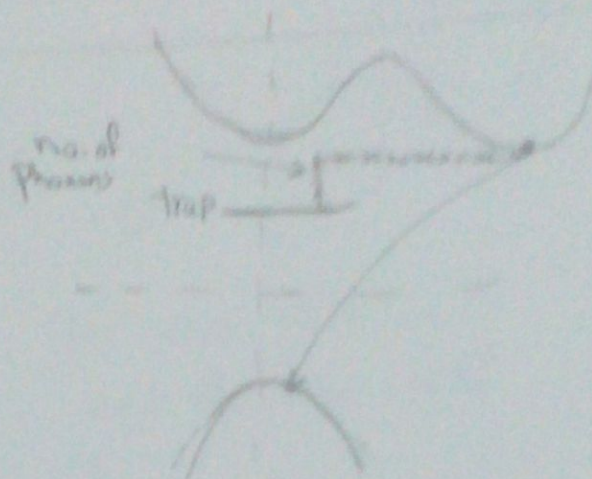
↳ no trap state in Band Gap



↳ Absorption or emission can occur

### Non-radiative

↳ Trap state in Band Gap

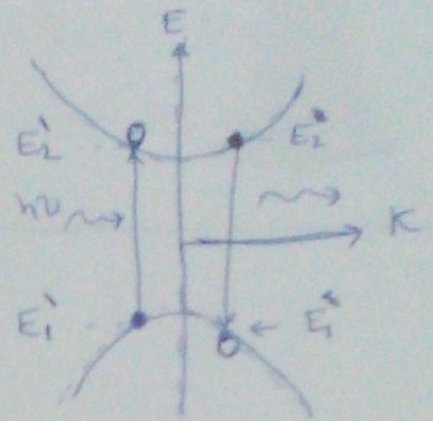


↳ Recombination with hole can occur in trap state by losing photons



## Probability of Emission and absorption

→ In emission, you need electron state in  $(E_2)$  and make transition to  $(E_1)$  (hole)



$$P_e = f(E_2) [1 - f(E_1)] \rightarrow ①$$

~~$P_a = f(E_1) [1 - f(E_2)]$~~  In absorption, you need hole in  $E_1$  and electron in  $E_2$

$$P_a = f(E_1) [1 - f(E_2)] \rightarrow ②$$

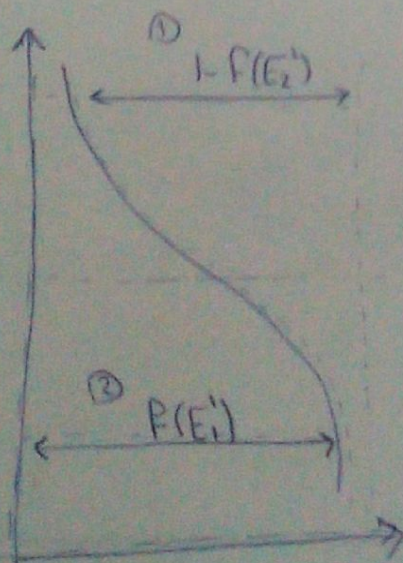
Absorption  
~~radiation~~

الحساب لاحتقال ال Emission

Source  $\rightarrow$  Emission  $\rightarrow P_e > P_a \rightarrow$  اقتر ال Emission  
detector  $\rightarrow$  absorption  $\rightarrow P_a > P_e \rightarrow$  اقتر ال absorption

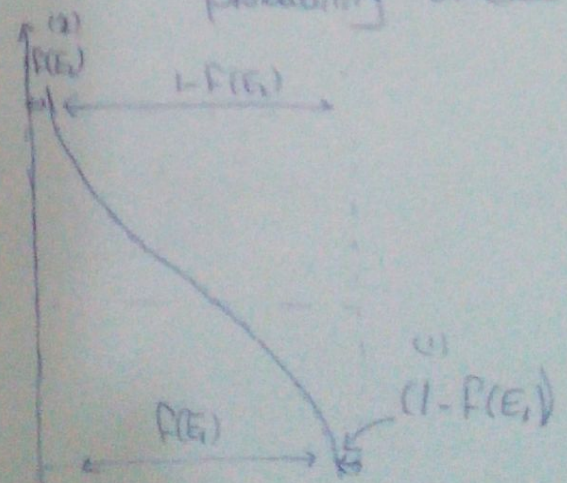
Case (i) Thermal Equilibrium (one Fermi function describe probability of electron)

Absorption



$P_A = ① \times ② \rightarrow$  large

$$P_e < P_a$$



$P_e = ① \times ② \rightarrow$  small



# # Double Hetero structure :

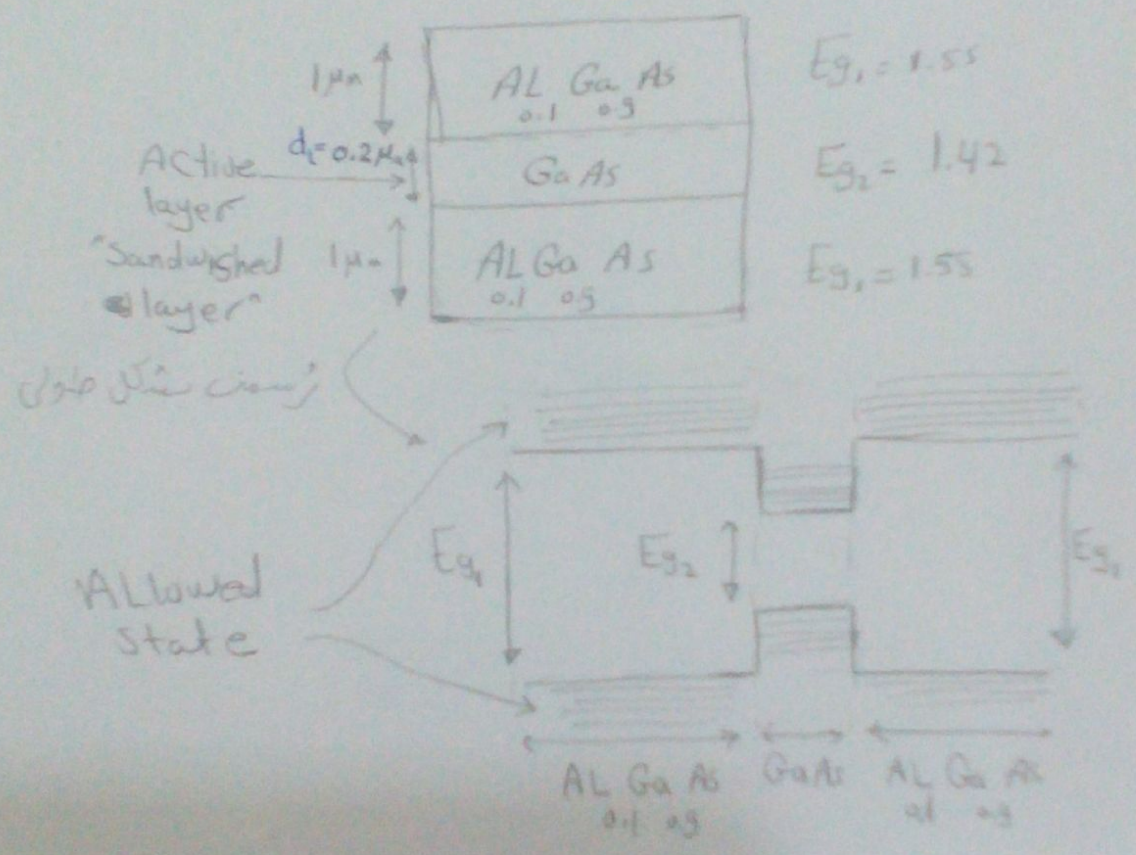
define as Two Semi Conductor materials grown into a Sandwich Layer.

outer layer  $\rightarrow$  material has  $E_{g1}$

Sandwiched layer  $\rightarrow E_{g2}$

$\& |E_{g2} \ll E_{g1}|$

Ex



Bulk material  $\rightarrow$   $1 \mu m$  layer  $\rightarrow$   $d = 0.2 \mu m$

Allowed state  $\rightarrow$   $V.B.L \ C.B$

if  $dL < \lambda$   $\leftarrow$  debraglie wavelength  $\rightarrow$  Quantum well structure

Structure التي يظهر على  $dL < \lambda$